

# A study on the optical properties of a novel flower-core photonic crystal fiber infiltrated with CCl<sub>4</sub>

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## ABSTRACT

A novel design of a photonic crystal fiber with a flower core is proposed for the first time to optimize dispersion suitable for broadband supercontinuum generation. The numerical simulation of the propagation of light modes in optical fibers is computed by solving Maxwell's wave equations with the full-vector finite-difference eigenmode method. As a result, near-zero ultraflat all-normal and anomalous dispersion was achieved with fluctuations of  $\pm 0.978$  ps/nm.km in the 294 nm wavelength region and  $\pm 1.168$  ps/nm.km in the 432 nm wavelength region, respectively. The combination of CCl<sub>4</sub> infiltration into the hollow core and the air hole size heterogeneity in the cladding also enhances the nonlinear properties of the fibers. Effective mode areas less than  $2 \mu\text{m}^2$  at the pump wavelength can help the supercontinuum spectrum broaden further toward the red wavelength region. Three fibers with structural parameters  $\Lambda = 0.8 \mu\text{m}$ ,  $d_1/\Lambda = 0.45$ ,  $\Lambda = 0.9 \mu\text{m}$ ,  $d_1/\Lambda = 0.5$ ,  $\Lambda = 0.9 \mu\text{m}$ , and  $d_1/\Lambda = 0.45$  are proposed for supercontinuum generation with low peak power due to nonlinear coefficients as high as hundreds of  $\text{W}^{-1} \cdot \text{km}^{-1}$ . These new optical fibers could be highly efficient laser sources that replace traditional glass-core optical fibers.

**Key words:** Flower-core PCFs, CCl<sub>4</sub> infiltration, ultraflat dispersion, high nonlinear coefficient, small effective mode area, low confinement loss, supercontinuum generation

## INTRODUCTION

In recent years, hollow-core photonic crystal fibers (HPCFs) infiltrated with highly nonlinear liquids have been an excellent alternative to glass-core fibers, as they are particularly suitable for generating supercontinuum (SCG). This is because the nonlinear refractive index of these liquids is much higher when compared with fused silica, even up to 100 times greater than<sup>1</sup>. The flat dispersion with a low value, small effective mode area, high nonlinear coefficient, and low loss are all essential factors in improving SCG efficiency, which has been verified in HPCFs infiltrated with toluene (C<sub>7</sub>H<sub>8</sub>), chloroform (CHCl<sub>3</sub>), benzene (C<sub>6</sub>H<sub>6</sub>), nitrobenzene (C<sub>6</sub>H<sub>5</sub>NO<sub>2</sub>), and tetrachloroethylene (C<sub>2</sub>Cl<sub>4</sub>)<sup>2-9</sup>. The outstanding advantages of SCGs include the further spectral expansion in the near-infrared region, high-coherent spectrum, smoothness, low noise, and flat-top, making them have a wide range of applications in the fields of optical communication, fiber optic sensing, optical coherence tomography, optical metrology and spectroscopy<sup>10-14</sup>.

The continuous development of fiber optic technology and the introduction of new materials are endless sources of inspiration for researchers in the design of novel optical fibers. Accordingly, the structural parameters of HPCFs are also always targeted to

drastically change the optical properties of the fibers, which is beneficial for different applications. Many previous publications have mentioned different fiber designs, such as substrates or composites for whole or part of the optical fiber<sup>15,16</sup>, cross-sections with different geometries<sup>17</sup>, changes in the core diameter, air hole diameter, and the distance between two adjacent air holes<sup>3,4,7,9</sup>. This study is also one such motivation, and we propose flower-core HPCFs filled with carbon tetrachloride (CCl<sub>4</sub>) as a novel fiber for potential nonlinear applications. CCl<sub>4</sub> is a very interesting nonlinear liquid, and its nonlinear refractive index is 5 times higher than that of silica<sup>1</sup>, which will create a large difference in the refractive index between the cladding and the core, causing the light modes to be confined better in the core. Moreover, its low toxicity (compared to liquids such as carbon disulfide, nitrobenzene, and toluene<sup>18</sup>) ensures safety in fiber fabrication. In particular, CCl<sub>4</sub> and silica have similar linear refractive indices<sup>19</sup>, which will enhance the coupling efficiency in all-fiber pump laser systems. Several previous papers have demonstrated the ability to achieve a broad SCG spectrum using silica-based HPCFs infiltrated with CCl<sub>4</sub>. Hexagonal, circular, and square lattices are quite commonly modeled. A flat all-normal dispersion with a value of  $-4.37$  ps/nm.km at a pump wavelength of  $1.55 \mu\text{m}$  was used

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to emit broadband SCG<sup>20</sup>. Experimentally, article<sup>21</sup> showed that the ability to obtain all-normal dispersion varies from  $-150$  to  $0$  ps/nm.km in the wide wavelength region. The effective mode area of  $42.2 \mu\text{m}^2$  and the nonlinear coefficient of  $221 \text{ W}^{-1}.\text{km}^{-1}$  contributed to the spectral expansion spanning from  $850$  to  $1250$  nm. The flat dispersion and characteristic quantities with values suitable for SCG spectral expansion are also reported experimentally in paper<sup>22</sup>. However, the values of the quantities characteristic in these reports have not been optimized simultaneously. The nonlinear coefficients of HPCFs are still low, and the effective mode area is still large, which causes the SCG spectrum to not broaden as expected<sup>20</sup>. To eliminate such limitations, a different approach in HPCF design with differences in the air hole size in the cladding was presented<sup>23,24</sup>. Two optimized HPCFs with flat all-normal and anomalous dispersion and low values of  $-9.376$  and  $1.015$  ps/nm.km enabled SCG spectra as broad as  $768$  and  $1751.1$  nm with flat-top<sup>23</sup>. Similarly, work<sup>24</sup> also demonstrates the ability to achieve HPCFs with low dispersion, small effective mode area, and low confinement loss.

Our new design combines two methods. First, the hollow flower-core infiltrate to  $\text{CCl}_4$  will create a large difference between the refractive index of the core and the cladding. Second, the air hole in the first ring is smaller than the others, making it easy to control dispersion and loss. Thus, we obtained ultraflat dispersions with variable values of  $\pm 0.978$  ps/nm.km and  $\pm 1.168$  ps/nm.km in the wavelength regions of  $294$  nm and  $432$  nm, respectively, for optimal optical fibers. In addition, the nonlinear properties of the proposed fibers are also analyzed in detail to guide SCGs with low peak power.

### MATERIALS-METHODS

The idea of designing these HPCFs is based on works<sup>3,6,24</sup> and<sup>25</sup>, which emphasize the role of the size of the air holes in the cladding. The dispersion properties can be easily controlled if the air hole in the first ring is not the same as the others. The loss in the fundamental mode or higher-order modes can be improved by the influence of subsequent rings. Therefore, the air holes in the first ring are designed with diameter  $d_1$ , which is smaller than  $d_2$  ( $d_2$  is the diameter of the other holes). The distance between two adjacent air holes is pitch  $\Lambda$ , and the hollow core has diameter  $D_c$ . The design parameters are shown in Table 1. Figure 1a shows the cross-sectional view of the HPCF with a flower-shaped hollow core. The lattice has a regular hexagonal structure with a flower-shaped core

being the largest air hole in the center filled with  $\text{CCl}_4$ . The first ring in the cladding has six small air holes evenly spaced around the core. The air holes in the other seven rings are larger in size and are designed parallel to the axis of the core. Figure 1b confirms the well-confined light modes in the core of the HPCF with  $\Lambda = 0.8 \mu\text{m}$  and  $d_1/\Lambda = 0.45$ .

Maxwell's wave equations are used to calculate the propagation coefficients and modes of electromagnetic fields in HPCFs using Lumerical Mode Solutions (LMS) software. The boundary conditions are perfectly matched layers that are subdivided to reduce the loss to the smallest possible value. The cross-section of HPCFs is approximately a few micro  $\mu\text{m}^2$ , which is divided into hundreds of thousands of rectangles to reduce the meshing error of the simulations. The optical properties of the HPCFs are simulated through the LMS with the full-vector finite-difference eigenmode (FDE) method. Fused silica and  $\text{CCl}_4$  were established and entered into the LMS by declaring the Sellmeier and Cauchy coefficients from Equations (1) and (2)<sup>26,27</sup>. It is not too difficult to experimentally fabricate  $\text{CCl}_4$ -infiltrated HPCFs. The stack-and-draw method is commonly used for spinning, while the fluids are introduced into the core via a pump system with a laser writing technique or a thermal fusion splicer<sup>22,28</sup>. Figure 1c shows that the linear refractive index of fused silica and  $\text{CCl}_4$  both decrease with wavelength and that the difference in the index of the two materials is not too large.

$$n_{\text{CCl}_4}^2(\lambda) = 2.085608282 + 0.0053373\lambda^2 + 0.012201206\lambda^{-2} + 0.000056451\lambda^{-4} + 0.000048106\lambda^{-6}, \tag{1}$$

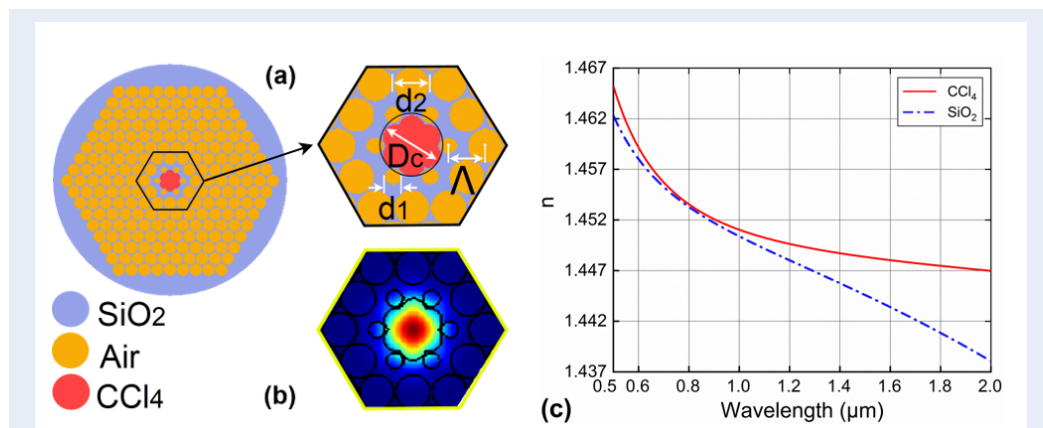
$$n_{\text{SiO}_2}^2(\lambda) = 1 + \frac{0.6961663\lambda^2}{\lambda^2 - 0.0684043^2} + \frac{0.4079426\lambda^2}{\lambda^2 - 0.1162414^2} + \frac{0.8974794\lambda^2}{\lambda^2 - 9.896161^2}, \tag{2}$$

where  $\lambda$  is the wavelength and  $n(\lambda)$  is the linear refractive index of the materials.

The dispersion is the fast or slow propagation over time of different frequency components of a light pulse in a nonlinear optical medium such as an optical fiber. This is the result of the interaction of light with electrons in the medium. It is an important parameter that governs the efficiency of the SCG generation process. The flatness over a wide wavelength range, low dispersion gradient, small dispersion value, all-normal or anomalous nature of dispersion, and shift of zero dispersion wavelength (ZDW) have always been the first goals of optical fiber designs in theoretical simulations as well as experiments. The dispersion

**Table 1: The structural parameters of HPCFs with CCl<sub>4</sub> infiltration**

d1/Λ	Λ = 0.8 μm			Λ = 1.5 μm		
	d1 (μm)	d2 (μm)	Dc (μm)	d1 (μm)	d2 (μm)	Dc (μm)
0.3	0.24	0.76	1.48	0.45	1.43	2.78
0.35	0.28	0.76	1.45	0.53	1.43	2.71
0.45	0.36	0.76	1.37	0.68	1.43	2.56
0.5	0.40	0.76	1.32	0.75	1.43	2.48
0.55	0.44	0.76	1.27	0.83	1.43	2.38
0.6	0.48	0.76	1.22	0.90	1.43	2.28
0.65	0.52	0.76	1.16	0.98	1.43	2.17
	Λ = 0.9 μm			Λ = 2.0 μm		
0.3	0.27	0.86	1.67	0.60	1.90	3.70
0.35	0.32	0.86	1.63	0.70	1.90	3.62
0.45	0.41	0.86	1.54	0.90	1.90	3.42
0.5	0.45	0.86	1.49	1.00	1.90	3.30
0.55	0.50	0.86	1.43	1.10	1.90	3.18
0.6	0.54	0.86	1.37	1.20	1.90	3.04
0.65	0.59	0.86	1.30	1.30	1.90	2.90



**Figure 1:** The cross-sectional view of the HPCF, flower-shaped hollow core in the center, surrounded by six air holes of smaller size, the remaining air holes are arranged regularly into 7 rings in the cladding (a). The linear refractive index of fused silica and CCl<sub>4</sub> varies with wavelength (b).

is calculated through the real part of the effective refractive index ( $\text{Re}[n_{eff}]$ ), the wavelength ( $\lambda$ ), and the speed of light in a vacuum ( $c$ ) according to the following formula<sup>29</sup>:

$$D_c = -\frac{\lambda}{c} \frac{d\text{Re}[n_{eff}]}{d\lambda^2}. \quad (3)$$

The nonlinearity of optical fibers is characterized by a number of characteristic quantities, such as the nonlinear coefficient ( $\gamma$ ), effective mode area ( $A_{eff}$ ), and confinement loss ( $L_c$ ). They are computed through the equations below<sup>29</sup>. The properties of the SCG spectrum are strongly influenced by these quantities, but it is difficult to optimize them simultaneously. The more relevant values are, the more beneficial the SCG.

$$\gamma(\lambda) = 2\pi \frac{n_2}{\lambda A_{eff}}, \quad (4)$$

where  $n_2$  is the nonlinear refractive index of fused silica.

$$A_{eff} = \frac{(\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |E|^2 dx dy)^2}{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |E|^4 dx dy} \quad (5)$$

$$L_c = 8.686 \frac{2\pi}{\lambda} \text{Im}[n_{eff}], \quad (6)$$

where  $\text{Im}[n_{eff}]$  is the imaginary part of the effective refractive index.

## RESULTS

The diversity in dispersion is the expected result for  $\text{CCl}_4$ -infiltrated flower-core HPCFs. All-normal and anomalous dispersions with one or more ZDWs are found with different fiber structures, demonstrating that the structural parameters ( $d_1/\Lambda$  and  $\Lambda$ ) strongly influence the dispersion properties (Figure 2). When  $\Lambda = 0.8 \mu\text{m}$ , there are three anomalous dispersion curves with small  $d_1/\Lambda$  ( $d_1/\Lambda = 0.3, 0.35, 0.4$ ). They intersect the zero dispersion line at a point corresponding to the ZDW. Moreover, these ZDWs shift toward a longer wavelength range as  $d_1/\Lambda$  increases. Increasing  $d_1/\Lambda$  further, the dispersion curves are increasingly compressed down from the zero dispersion line, becoming all-normal dispersion properties. In particular, we obtained a near-zero ultraflat all-normal dispersion curve with the structure  $d_1/\Lambda = 0.45$ , the range of variation  $\pm 0.978 \text{ ps/nm.km}$  spanning from the wavelength 1379 nm to 1673 nm. Increasing  $\Lambda$  to  $0.9 \mu\text{m}$ , the dispersion curves tend to shift above the zero dispersion line, all of which are anomalous dispersion curves with one ZDW ( $d_1/\Lambda \leq 0.45$ ) and two ZDWs ( $d_1/\Lambda \geq 0.5$ ). The HPCF with structure  $\Lambda = 0.9 \mu\text{m}$  and  $d_1/\Lambda = 0.5$  is the flattest anomalous dispersion curve, and the dispersion value

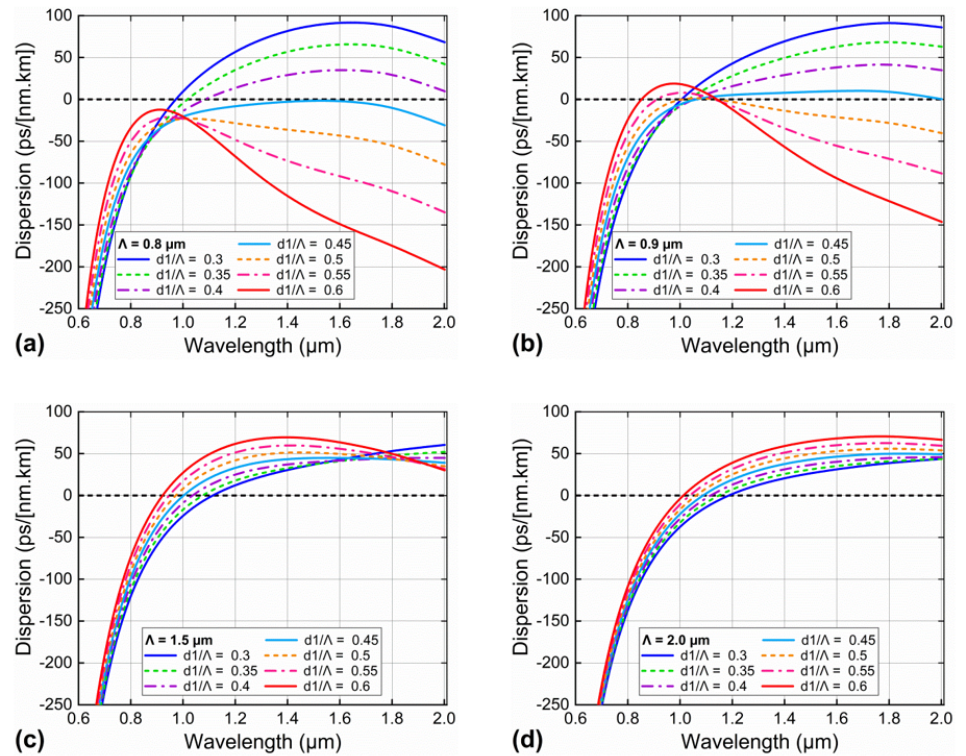
varies  $\pm 1.168 \text{ ps/nm.km}$  in the wavelength range of 1420–1852 nm. Continuing to increase  $\Lambda$  ( $\Lambda = 1.5$  and  $2.0 \mu\text{m}$ ), the all-normal dispersion curves no longer appear. Instead, all curves are anomalous dispersions with ZDW shifting to the short wavelength region when the value of  $d_1/\Lambda$  rises. Table 2 illustrates the values of ZDW according to the variation in  $d_1/\Lambda$ . The shift of ZDW toward long wavelengths is very significant in selecting suitable pump wavelengths for SCG generation. HPCFs with ZDW closer to  $1.55 \mu\text{m}$  are beneficial factors because this is the wavelength of commercially available lasers. The dispersion values are also calculated at a wavelength of  $1.55 \mu\text{m}$ , as verified in Table 3.

Based on preliminary results on dispersion properties, we proposed three HPCFs with suitable dispersion characteristics for detailed analysis and orientation for SCG application (Figure 3a). They are #F<sub>1</sub> ( $\Lambda = 0.8 \mu\text{m}$ ,  $d_1/\Lambda = 0.45$ ), #F<sub>2</sub> ( $\Lambda = 0.9 \mu\text{m}$ ,  $d_1/\Lambda = 0.5$ ), and #F<sub>3</sub> ( $\Lambda = 0.9 \mu\text{m}$ ,  $d_1/\Lambda = 0.45$ ). The confinement loss, effective mode area, and nonlinear coefficient are calculated with the results shown in Figure 3b-d. The structural parameters and the values of the characteristic quantities at the pumping wavelength of the three optimal wavelengths are presented in Table 4. The way to select the appropriate pump wavelength for SCGs using the three proposed structures must be based on the following: First, the value of the dispersion, which is sufficiently small or close to the ZDW for anomalous dispersions, or a value close to the local maximum of the all-normal dispersion curve. Second, match the pump wavelengths of commercial laser sources. Therefore, the selected pump wavelengths are  $1.55 \mu\text{m}$  for the #F<sub>1</sub> fibers and  $1.064 \mu\text{m}$  for the #F<sub>2</sub> and #F<sub>3</sub> fibers.

## DISCUSSION

The diversity in dispersion results of  $\text{CCl}_4$ -infiltrated HPCFs opens up many opportunities for SCG applications for both anomalous and all-normal dispersion. We obtained two near-zero ultraflat dispersions for both all-normal ( $\Lambda = 0.8 \mu\text{m}$ ,  $d_1/\Lambda = 0.45$ ) and anomalous ( $\Lambda = 0.9 \mu\text{m}$ ,  $d_1/\Lambda = 0.45$ ) (Figure 2a, b) with low dispersion values. This is significant because previous publications on  $\text{CCl}_4$ -infiltrated HPCFs have yet to find such dispersions, although every design effort has been performed to control dispersion<sup>20–24,30</sup>.

The different dispersion properties will be responsible for different SCG spectral characteristics. To obtain a wide SCG spectrum, low noise, high coherence, and flat-top, it is common to pump the fiber in the all-normal dispersion regime. Then, the soliton dynamics, especially the separation of higher-order solitons



**Figure 2:** The dispersion against wavelength with HPCFs of different structure parameters, the filling factor  $d_1/\Lambda$  varies from 0.3 to 0.6, with  $\Lambda = 0.8 \mu\text{m}$  (a),  $0.9 \mu\text{m}$  (b),  $1.5 \mu\text{m}$  (c), and  $2.0 \mu\text{m}$  (d)

**Table 2:** The ZDW values of infiltrated- $\text{CCl}_4$  HPCFs with variations in  $\Lambda$  and  $d_1/\Lambda$

	$\Lambda = 0.8 \mu\text{m}$	$\Lambda = 0.9 \mu\text{m}$		$\Lambda = 1.0 \mu\text{m}$	$\Lambda = 1.5 \mu\text{m}$
$d_1/\Lambda$	ZDW <sub>s1</sub>	ZDW <sub>s1</sub>	ZDW <sub>s2</sub>	ZDW <sub>s1</sub>	ZDW <sub>s1</sub>
0.3	0.972	1.005		1.113	1.185
0.35	1.016	1.031		1.074	1.147
0.4	1.083	1.05		1.034	1.116
0.45	D < 0	1.062		1.001	1.086
0.5	D < 0	1.006	1.137	0.971	1.06
0.55	D < 0	0.91	1.133	0.946	1.035
0.6	D < 0	0.85	1.142	0.921	1.012

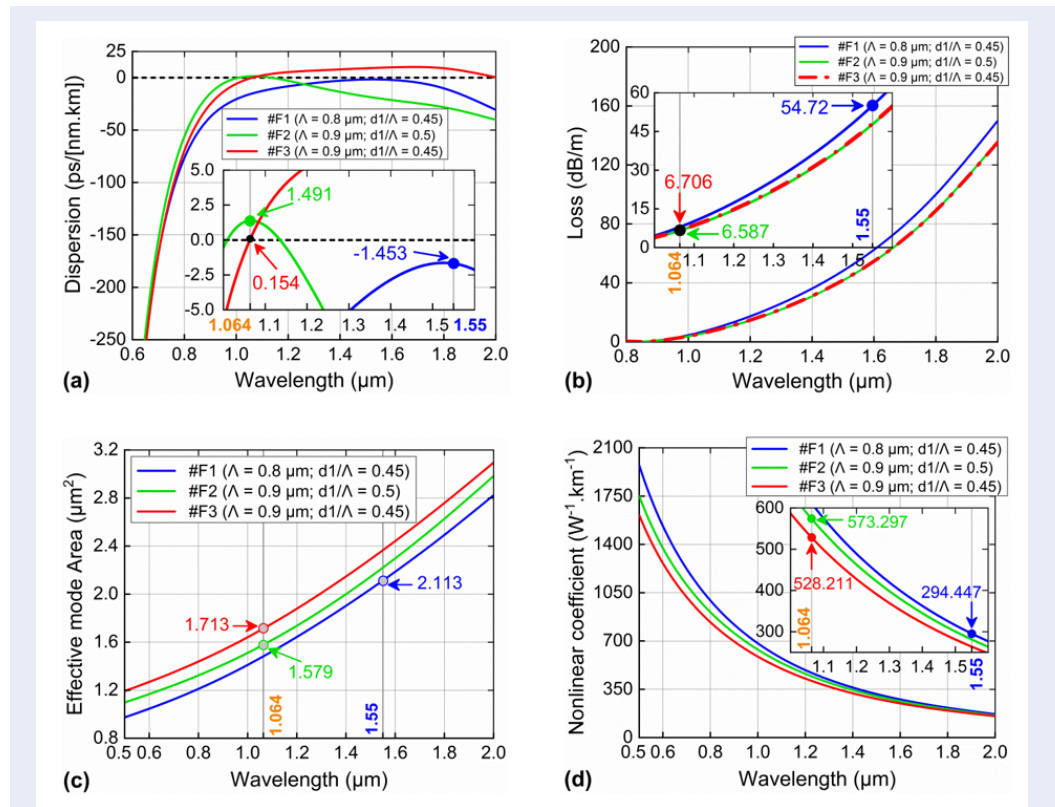
from the elementary solitons, which are responsible for the noise of the spectrum, are suppressed<sup>31</sup>. In this case, four-wave mixing and self-phase modulation followed by optical wave breaking are the main mechanisms that strongly influence spectral expansion. In contrast, very large SCG bandwidths, even several octaves, can be achieved thanks to the dominance of soliton-related effects such as soliton fission, soliton self-frequency shift, and blueshifted dispersive

waves<sup>31</sup>, but the spectrum is very noisy and has low coherence.

#F<sub>1</sub> fiber with an all-normal dispersion profile, dispersion variation as small as  $\pm 0.978$  ps/nm.km in the 294 nm wavelength range, and dispersion value of  $-1.453$  ps/nm.km is expected to generate a smooth, noiseless, broad spectrum SCG at a  $1.55 \mu\text{m}$  pump wavelength. Such SCGs will have high potential in applications such as optical coherence tomography,

**Table 3:** Dispersion values at 1.55 μm of infiltrated CCl<sub>4</sub> HPCFs with variations in Λ and d<sub>1</sub>/Λ

d <sub>1</sub> /Λ	D (ps/nm.km)			
	Λ = 0.8 μm	Λ = 0.9 μm	Λ = 1.0 μm	Λ = 1.5 μm
0.3	90.691	82.299	40.084	29.149
0.35	64.936	60.609	39.292	33.447
0.4	34.861	36.562	41.034	38.812
0.45	-1.453	9.496	44.973	45.024
0.5	-41.27	-19.829	50.746	51.789
0.55	-87.731	-51.2	57.746	58.828
0.6	-141.968	-86.376	66.199	66.914



**Figure 3:** The wavelength-dependent characteristic quantities of the three proposed HPCFs, #F<sub>1</sub> (Λ = 0.8 μm, d<sub>1</sub>/Λ = 0.45), #F<sub>2</sub> (Λ = 0.9 μm, d<sub>1</sub>/Λ = 0.5), and #F<sub>3</sub> (Λ = 0.9 μm, d<sub>1</sub>/Λ = 0.45). (a) The dispersion versus wavelength curve, the right inset illustrates the dispersion values at the pump wavelength. (b) The confinement loss is a function of wavelength, the left inset shows the L<sub>c</sub> values at the pump wavelength. (c) The effective mode area increases with wavelength, the A<sub>eff</sub> values at the pump wavelength are also testified on the graphs. (d) The nonlinear coefficient is wavelength dependent, the right inset displays the γ values at the pump wavelength.

**Table 4: The structural parameters and the values of the characteristic quantities at the pump wavelength of the three proposed HPCFs**

#	$D_c$	$\Lambda$	$d_1/\Lambda$	Pump wavelength	$Re[n_{eff}]$	D	$L_c$	$A_{eff}$	$\gamma$
	( $\mu\text{m}$ )	( $\mu\text{m}$ )		( $\mu\text{m}$ )	(real)	(ps/nm.km)	(dB/m)	( $\mu\text{m}^2$ )	( $\text{W}^{-1}.\text{km}^{-1}$ )
#F1	1.366	0.8	0.45	1.55	1.326	-1.453	54.72	2.113	294.447
#F2	1.485	0.9	0.5	1.064	1.383	1.491	6.587	1.579	573.297
#F3	1.537	0.9	0.45	1.064	1.388	0.154	6.706	1.713	528.211

spectroscopy and metrology<sup>32</sup>. The #F<sub>2</sub> fiber has anomalous dispersion with two very close ZDWs of 1.006  $\mu\text{m}$  and 1.137  $\mu\text{m}$  (Table 2). Although a pump wavelength of 1.064  $\mu\text{m}$  is chosen in the anomalous dispersion region and a small dispersion value of 1.491 ps/nm.km, the obtained SCG spectra would be in stark contrast to standard photonic crystal fibers that have anomalous dispersion with only one ZDW or two ZDWs far apart<sup>15,33</sup>. In such fibers, the Four-Wave Mixing effect becomes a major factor that makes the SCG spectrum broader while the soliton dynamics are captured and play a barely significant role in the formation of the supercontinuum<sup>15</sup>. The spectral characteristics are similar to those of SCG using fibers with all-normal dispersion. The #F<sub>3</sub> fiber has a near-zero ultraflat anomalous dispersion profile with one ZDW, and the pumping wavelength is 1.064  $\mu\text{m}$  larger than that of ZDW (1.062  $\mu\text{m}$ ), which will enable a very broad SCG spectrum, broader than the two fibers #F<sub>1</sub> and #F<sub>2</sub>, but the spectrum will be much noisier. Of the three proposed fibers, the dispersion value at the pump wavelength of the #F<sub>3</sub> fiber is 0.154 ps/nm.km, which is nearly 10 times smaller than that of #F<sub>1</sub> and #F<sub>2</sub> (Table 4). In addition, the dispersion values obtained for these three optimal fibers are hundreds of times smaller than those in work<sup>21</sup>. Compared with paper<sup>20</sup>, the #F<sub>1</sub> and #F<sub>2</sub> fibers have an approximately three times smaller dispersion at the pump wavelength. The small dispersion value of the #F<sub>3</sub> fiber at the pump wavelength will be a good condition to broaden the SCG spectrum more than previously published. This value is between 6.5 and 60 times smaller than the optimal optical fibers verified in work<sup>24</sup>.

The confinement loss is the loss that should be minimized during the simulation of HPCFs to ensure that the power of the propagation is not reduced. It is a loss that is incurred due to leakage of modes from the core to the cladding or between the air holes or due to the imperfect structure of the optical fibers. Therefore, the confinement loss is affected by the wavelength,

pitch  $\Lambda$ , number of air hole rings, and air hole size. Figure 3b shows that the low-frequency components (long wavelength) leak more so that  $L_c$  increases in this wavelength region. In the short wavelength region, the  $L_c$  of the three fibers is quite similar ( $\lambda < 1.0 \mu\text{m}$ ), but the difference in values is larger in the longer wavelength region. The #F<sub>1</sub> fiber has a larger  $L_c$  in the wavelength range  $\lambda > 1.0 \mu\text{m}$ , while the  $L_c$  of the other two fibers is almost the same. For the three proposed fibers, the  $L_c$  value at the pump wavelengths is quite suitable for SCG application. Fiber #F<sub>1</sub> has the highest  $L_c$  of 54.72 dB/m compared to the other two fibers, and #F<sub>2</sub> and #F<sub>3</sub> have  $L_c$  values of 6.587 and 6.706 dB/m, respectively (Table 4). Thus, the SCG progress using the #F<sub>1</sub> fiber will probably be more limited in extending the spectrum toward the red wavelength region compared to #F<sub>2</sub> and #F<sub>3</sub>. In comparison with #SF<sub>1</sub>, #SF<sub>2</sub>, and #CF<sub>2</sub> fibers with square and circular lattices in publication<sup>24</sup>, the  $L_c$  values of #F<sub>2</sub> and #F<sub>3</sub> fibers are approximately 2.5 to 4 times smaller.

The effective mode area is related to the energy density of the light mode per unit length of the fiber and its maximum energy density.  $A_{eff}$  increases as the wavelength increases, as shown in Figure 3c. Longer wavelengths are more difficult to confine to the core than shorter wavelength components. In addition, the core size is also a parameter that affects the value of  $A_{eff}$ . Smaller cores often exhibit better light restriction in the core, although being too small makes fiber fabrication more difficult. The #F<sub>1</sub> fiber has the smallest  $A_{eff}$  in the investigated wavelength region due to having the smallest core ( $D_c = 1.366 \mu\text{m}$ ) (Table 4). This leads to its highest nonlinear coefficient in the entire wavelength range (Figure 3d) because the two quantities are inversely proportional to each other. However, at a pump wavelength of 1.55  $\mu\text{m}$ , this fiber has  $\gamma = 294.447 \text{ W}^{-1}.\text{km}^{-1}$ , which is less high than that of fibers #F<sub>2</sub> and #F<sub>3</sub> (573.297 and 528.211  $\text{W}^{-1}.\text{km}^{-1}$ ) because their  $\gamma$  is chosen at the pump wavelength of 1.064  $\mu\text{m}$ . The high value of  $\gamma$  contributes to the broadened SCG spectrum with low input pulse peak

**Table 5: The characteristic quantities at the pump wavelength of three proposed HPCFs in comparison with some previous work on liquid-filled HPCFs**

#	Refs.	Pump wave-length ( $\mu\text{m}$ )	D (ps/nm.km)	$L_c$ (dB/m)	$A_{eff}$ ( $\mu\text{m}^2$ )	$\gamma$ ( $\text{W}^{-1}.\text{km}^{-1}$ )
#F1	This work	1.55	-1.453	54.72	2.113	294.447
#F2	This work	1.064	1.491	6.587	1.579	573.297
#F3	This work	1.064	0.154	6.706	1.713	528.211
$\text{CCl}_4$ , #F <sub>1</sub>	20	1.35	12	—	—	—
$\text{CCl}_4$ , #F <sub>2</sub>		1.55	-4.37	—	10.58	—
$\text{CCl}_4$ , #SF <sub>1</sub>	24	1.095	-6.577	17.833	2.186	404.924
$\text{CCl}_4$ , #SF <sub>2</sub>		1.30	1.331	28.186	10.479	84.493
$\text{CCl}_4$ , #CF <sub>1</sub>		0.98	-9.376	4.545	1.513	585.025
$\text{CCl}_4$ , #CF <sub>2</sub>		1.30	1.015	19.406	8.735	101.371
$\text{C}_7\text{H}_8$ , #F <sub>1</sub>	3	1.55	0.489	—	2.527	2699.919
$\text{C}_7\text{H}_8$ , #F <sub>2</sub>		1.55	-1.534	—	2.632	2592.282
$\text{CHCl}_3$ , #F <sub>1</sub>	4	0.945	-1.629	2.477	1.43	763.313
$\text{CHCl}_3$ , #F <sub>2</sub>		1.40	2.619	39.628	11.524	63.913
$\text{C}_2\text{Cl}_4$ , #F <sub>1</sub>	8	1.56	-15.0	4.0	433.2	156.9
$\text{C}_2\text{Cl}_4$ , #F <sub>2</sub>		1.56	3.20	4.2	16.67	40.79
$\text{C}_2\text{Cl}_4$ , #F <sub>3</sub>		1.03	-4.85	5.3	359.1	189.3

power (the femtosecond duration and nano Joule energy)<sup>3,4,8,9</sup>. The proposed three fibers also provide smaller  $A_{eff}$  and higher  $\gamma$  values than some of the optical fibers in previous publications of  $\text{CCl}_4$ -filled HPCF<sup>20-24</sup>. Even when compared with HPCFs infiltrated with other nonlinear liquids, we obtain a better characteristic quantity at the pump wavelength. The results of this comparison are presented in Table 5.

### CONCLUSIONS

We designed a novel structure of hexagonal lattice photonic crystal fiber with a flower-shaped hollow core filled with  $\text{CCl}_4$ . The dispersion and nonlinear properties of the fiber are investigated by numerical simulation based on solving Maxwell's wave equations with the FDE method. Some of the outstanding results of this work are as follows:

First, a near-zero ultraflat all-normal dispersion with small fluctuations of  $\pm 0.978$  ps/nm.km, covering the wavelength region 1379–1673 nm, is achieved with  $\Lambda = 0.8 \mu\text{m}$  and  $d_1/\Lambda = 0.45$ .

Second, the structure  $\Lambda = 0.9 \mu\text{m}$ ,  $d_1/\Lambda = 0.45$  exhibits near-zero ultraflat anomalous dispersion with a variation value of  $\pm 1.168$  ps/nm.km, spanning from 1420

to 1852 nm.

Third, we propose three structures, #F<sub>1</sub>, #F<sub>2</sub>, and #F<sub>3</sub>, with flat dispersion and small values of -1.453, 1.491, and 0.154 ps/nm.km at wavelengths of 1.55, 1.064, and 1.064  $\mu\text{m}$ , respectively. In comparison with previous publications, we confirm that suitable characteristic quantities of these fibers, such as the small effective mode area, high nonlinear coefficient, and low confinement loss, are favorable conditions to generate broadband supercontinuum with low peak power.

We also analyzed the dispersion and nonlinear properties of the proposed three fibers in detail to guide the appropriate application of supercontinuum generation for each fiber type. The proposed fibers can be low peak power supercontinuum generation sources replacing traditional glass core fibers.

### ABBREVIATIONS

- SCG: Supercontinuum generation
- HPCFs: Hollow-core Photonic Crystal Fibers
- ZDW: zero dispersion wavelength
- LMS: Lumerical Mode Solutions
- FDE: Finite Difference Eigenmode



## COMPETING INTERESTS

The authors declare that they have no conflicts of interest.

## AUTHORS' CONTRIBUTIONS

Thuy Nguyen Thi: Designing and simulating the PCF structures, Data analysis, Data processing, Plotting graph, Methodology, Writing manuscript, Answering the reviewer's questions.

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