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Dependence on the Armchair/Zigzag Edge Ratio of the Melting Process of Armchair Hexagonal Boron Nitride Nanoribbon

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ABSTRACT The dependence of the melting point on the armchair/zigzag (A/Z) edge ratios in armchair hexag-

onal boron nitride nanoribbons (h-BNNR) is investigated through molecular dynamics simulations. For this purpose, initial configurations with eight different A/Z edge ratios (0.017377, 0.069510, 0.278481, 0.434782, 1.724409, 6.968254, 10.745098, and 43.88) of armchair h-BNNRs, each containing the same number of atoms (10,000 identical B and N atoms), are heated from 50 K to 7000 K using the Tersoff potential. The initial (0.017377 A/Z ratio) and the final (43.88 A/Z ratio) configurations significantly influence the melting process of the armchair h-BNNRs: The 0.017377 A/Z configuration exhibits a high melting point (5300 K) compared to the subsequent seven cases; the melting process in the 43.88 A/Z ratio configuration is markedly influenced by finite size effects. The melting points of the intervening six configurations are relatively unaffected by the A/Z edge ratio, with an average melting point of 4180 K for these configurations. When analyzing a system with 10,000 atoms, the critical A/Z edge ratio is identified at 10.745098. At this critical A/Z edge ratio, the melting point shows minor fluctuations around 4040 K when the number of atoms in the configuration is increased from 10,000 to 25,600 atoms. It is noted that, at this critical A/Z ratio, the melting point is not significantly affected by an increase in the number of atoms within the configuration.

Key words: Melting of armchair hexagonal boron nitride nanoribbon, A/Z edge ratio dependence, Critical armchair/zigzag edge ratio, Finite size effects

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¹ **INTRODUCTION**

- ² The remarkable properties of two-dimensional mate-³ rials have garnered considerable attention in recent ⁴ years, owing to their unique electronic, thermal, and ⁵ mechanical characteristics. Graphene, a single layer ⁶ of carbon atoms arranged in a hexagonal lattice, has ⁷ emerged as a revolutionary material with extraordi-⁸ nary properties, revolutionizing the landscape of ma- \circ terials science and technology^{[1](#page-6-0)}. Beyond graphene, ¹⁰ a rich family of two-dimensional materials, often re-¹¹ ferred to as "graphene-like" materials, has been dis-¹² covered, each with its own unique characteristics and ¹³ applications. Materials such as hexagonal boron ni-¹⁴ tride (h-BN)^{[2](#page-7-0)-5}, transition metal dichalcogenides^{[6](#page-7-2)[,7](#page-7-3)}, 15 and black phosphorus (phosphorene)^{[8](#page-7-4),[9](#page-7-5)} are among ¹⁶ the graphene-like materials that have garnered at-¹⁷ tention for their unique properties. h-BN, for in-¹⁸ stance, is an insulator with excellent thermal stabil-¹⁹ ity, serving as an ideal substrate for graphene-based 20 devices^{[5,](#page-7-1)[10](#page-7-6)[–13](#page-7-7)}. Armchair hexagonal boron nitride ²¹ nanoribbons (h-BNNR) are narrow strips of h-BN ²² with specific edge configurations that can be tailored
- 23 to exhibit distinct electronic behaviors $14-16$ $14-16$ $14-16$. There-²⁴ fore, armchair h-BNNR stands out as a promising

candidate due to its intriguing combination of prop- ²⁵ erties. 26

The thermal properties of armchair h-BNNR are 27 not only of fundamental interest but also hold sig- ²⁸ nificant practical implications for nanoelectronics^{[17](#page-7-10)}, 29 thermal management 18 , and materials science. As 30 the width of these nanoribbons is reduced towards the nanoscale, quantum size effects become increasingly pronounced, resulting in unique thermal behav- 33 i ors $19,20$ $19,20$. Additionally, the specific edge configura- 34 tions, whether zigzag or armchair, can have a pro- ³⁵ found impact on their thermal properties $11,21,22$ $11,21,22$ $11,21,22$ $11,21,22$. This 36 influence stems from the altered phonon dynamics, 37 lattice vibrations, and thermal transport mechanisms 38 at the edges of the ribbons.

Up to now, the implementation of the armchair h-BN melting process has encountered many challenges. 41 However, experimental results have been obtained for 42 h-BN in powder form. Powder h-BN has a high melting point, typically around 3000*◦*C (depending on the ⁴⁴ purity and crystalline structure)^{[23](#page-7-17)}. This high melt- 45 ing point is due to the strong covalent bonds between 46 boron and nitrogen atoms, similar to those in dia- ⁴⁷ mond and graphite in carbon-based materials. 48

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 Understanding the interplay between size, edge struc- ture, and thermal behavior in armchair h-BNNR is not only essential for fundamental insights into nanoscale heat transport but also holds the potential for the design of advanced nanomaterials with tailored thermal characteristics for diverse technologi- cal applications. In this study, by using molecular dy- namics (MD) simulation, we delve into the depen- dence of the melting process of armchair h-BNNR on the armchair/zigzag (A/Z) ratio and define the critical A/Z ratio. Note that the melting point of the configu- ration having this critical A/Z ratio will not be signifi- cantly affected when the number of atoms in the con- figuration is increased. Details on the calculation are given in Section 2. Results and discussion are shown in Section 3. Conclusions are presented in the last sec-tion of the paper.

⁶⁶ **CALCULATION**

 One of the critical aspects of MD simulations is the choice of interatomic potential functions, which gov- ern the interactions between particles in the simulated system. Among these potential functions, the Ter- soff potential stands out as a versatile and widely used model, particularly in the study of covalent and semi- covalent materials. Unlike simple pairwise poten- tials like Lennard-Jones, the Tersoff potential offers a more sophisticated description of bond-breaking and bond-forming events, capturing the intricacies of chemical bonding and the structural changes that oc- cur during the simulation. This potential model is particularly adept at reproduc- ing key material properties, including the prediction of lattice constants, elastic constants, phonon spectra, and defect energetics. Moreover, it excels in simu- lating complex phenomena like dislocations, chemi- cal reactions, and the mechanical behavior of materi- als under extreme conditions. The Tersoff potential's flexibility and versatility stem from its parametriza-87 tion, which allows researchers to tailor the potential parameters to specific materials and applications. In this study, the interactions between and in the initial configurations are described by Tersoff poten-⁹¹ tial ^{[24](#page-7-18)} which is written as below:

$$
E_b = \frac{1}{2} \sum_{i \neq j} f_c(r_{ij}) \left[f_R(r_{ij}) + b_{ij} f_a(r_{ij}) \right]. \tag{1}
$$

 $\frac{1}{2}$ Here, r_{ij} is the distance from atom i to atom j. The ⁹³ repulsive $f_R(r_{ij})$ and the attractive $f_a(r_{ij})$ terms are 94 based on Morse potential as proposed by Brenner^{[25](#page-7-19)}. ⁹⁵ The cutoff function using for calculating the number ⁹⁶ of neighbors as well as making the potential to zero σ outside the interaction shell is $f_c(r_{ij})$ term.

We use the software package Large-Scale Atomic/Molecular Massively Parallel Simulator to perform the MD simulation^{[26](#page-7-20)}. The ISAACS 100 software is used to calculated some thermal quan- 101 tities 27 . To visualize the atomic configuration, we 102 use VMD software 28 28 28 . The temperature inscrease as: 103 $T = T_0 + \gamma t$, in which, $T_0 = 50$ K is the initial value of 104 temperature of the simulation, is a heating rate, and t 105 is the time required for heating. Note that, the heating 106 rate in this study is 10^{12} K/s. To study the structural 107 characteristics at given temperatures, configurations ¹⁰⁸ are relaxed for 6×10^5 MD steps (0.0001 picoseconds 109 per step) to ensure the configuration stability.

To study the dependence on the A/Z edge ratio of h- ¹¹¹ BNNR melting process, all initial armchair h-BNNR 112 configurations have to be the same number of atoms ¹¹³ (10,000 atoms) but differ in zigzag- and armchair- ¹¹⁴ edge lengths. To keep the number of atoms of the ¹¹⁵ initial configurations being $10,000$ atoms, we have to 116 adjust the length of the armchair and zigzag edges as 117 shown in Table [1](#page-2-0). 118

The simulation passes some stages below: 119

i) To ensure the configuration stability, the initial con- 120 figurations are relaxed for MD steps at 50 K under pe- ¹²¹ riodic boundary conditions using canonical ensemble ¹²² simulation and the state of $\frac{1}{2}$

ii) To have armchair h-BNNR, non-periodic bound- ¹²⁴ ary conditions with an elastic reflection behavior are ¹²⁵ applied along the zigzag edges after adding a space of 126 20 Å at both ends. After that, initial configuration are 127 relaxed again to equilibrium further for MD steps at ¹²⁸ 50 K using canonical ensemble simulation 129

iii) The configurations are heated up to about 7000 130 K which is higher than the melting point of zigzag ¹³¹ h-BNNR 11 11 11 to ensure that at the chosen temperature 132 (7000 K) all configurations are in a liquid state. ¹³³

RESULTS AND DISCUSSION ¹³⁴

To study the thermodynamic properties of materials 135 upon heating, the total energy per atom plays a cru- ¹³⁶ cial role which helps in understanding how a material 137 responds to changes in temperature. Based on the to- ¹³⁸ tal energy per atom one can observe the phase tran- ¹³⁹ sitions and the temperature at the phase transitions 140 such as melting point. In this study, to investigate the 141 influence of armchair and zigzag edges on the melt- ¹⁴² ing process of armchair h-BNNR the total energy per ¹⁴³ atom of eight configurations in Table [1](#page-2-0) is calculated ¹⁴⁴ and presented in Figure [1.](#page-3-0) 145

Based on the results of the total energy per atom ¹⁴⁶ (square symbol in Figure [1\)](#page-3-0) one can see that except ¹⁴⁷ for Configuration 8 in Table [1](#page-2-0) (square symbol in Fig-ure [1](#page-3-0) h), the graphs of the total energy per atom of the $_{149}$

Table 1: The zigzag- and armchair-edge lengths of the armchair h-BNNR.												
Configurati 1		$\overline{2}$	3	$\overline{4}$	5	6	7	8				
Length (\AA)												
Zigzag- edge	22	44	88	110	219	439	548	1097				
Armchair- edge	1266	633	316	253	127	63	51	25				
A/Z ratio	0.017377	0.069510	0.278481	0.434782	1.724409	6.968254	10.745098	43.88				

other configurations in Table [1](#page-2-0) (square symbol in Fig- ure [1](#page-3-0) a-g) divide into two regions: i) In the first region, the graph of the total energy per atom for each configuration increases linearly to a certain value of tem- perature. This indicates that the configurations are in a crystal state. At this state, the atoms in the configurations oscillate about their equilibrium positions but these amplitudes of the vibration are not big enough to break the bonds between atoms. Therefore, the ma- terials are still in a crystal state; ii) Upon heating fur- ther, there is a sudden jump in the total energy per atom to a higher energy region. This behaviour of the total energy shows the phase transition often referred to as a first-order phase transition which is character- ized by a sudden and discontinuous change in total energy per atom.

¹⁶⁶ Related to Configuration 8 in Table [1,](#page-2-0) the behavior of the total energy per atom does not follow any rule ¹⁶⁸ maybe due to the strong effect of the edge size on the ¹⁶⁹ melting process of the configuration leading to the finite size effects.

171 One can see that the initial configurations are in a 172 crystal state. When these initial configurations are heated, the temperature in these configurations in-¹⁷⁴ creases until these configurations reach their melting ¹⁷⁵ point. At the melting point, these configurations start to absorb heat energy to undergo the phase transition 177 into a liquid state while the temperature remains con-¹⁷⁸ stant until the entire crystal structure has melted. Af-179 ter that, the temperature in these configurations in-¹⁸⁰ creases again. So, the change of the heat with respect ¹⁸¹ to the temperature (the heat capacity) shows a peak at ¹⁸² the melting point (the phase transition temperature). ¹⁸³ In general, the heat capacity is defined as below:

$$
C = \frac{\triangle E}{\triangle T} \tag{2}
$$

 In which, E is the total energy per atom, and T is tem- perature. In this context, the peak of the heat capacity can be used to define the melting point of the config-urations.

The heat capacity of eight configurations in Table [1](#page-2-0) is 188 calculated based on the total energy and is shown in ¹⁸⁹ Figure [1](#page-3-0) (solid line). The melting point of every con- ¹⁹⁰ figuration is defined at the peak of the heat capacity ¹⁹¹ line and presented in Table [2](#page-4-0).

Based on the results in Table [2](#page-4-0), we can point out the ¹⁹³ following key points: 194

i) As for Configuration [1](#page-2-0) in Table 1 (0.0173770 A/Z 195 edge ratio), the melting temperature (5300 K) is ¹⁹⁶ higher than the other ones (Table [2,](#page-4-0) Figure [1](#page-3-0)a). Mean- 197 while, regarding Configuration 8 in Table [1](#page-2-0) (43.88 198 A/Z edge ratio), the phase transition is complicated 199 due to the influence of finite size effects (Figure [1h](#page-3-0)). ²⁰⁰ The main reason here is the length of the armchair ²⁰¹ edges between configurations [1](#page-2-0) and 8 in Table 1. The 202 armchair length in Configuration 1 (0.0173770 A/Z ²⁰³ edge ratio) is too short compared to the zigzag edge. ²⁰⁴ As well known, compared to the zigzag edges, the ²⁰⁵ armchair edges contain more dangling bonds which ²⁰⁶ are unstable. This results in the armchair edges being 207 more susceptible to external factors than the zigzag ²⁰⁸ edges. Therefore, in Configuration [1](#page-2-0) in Table 1, the 209 length of the armchair edge is much shorter than the ²¹⁰ zigzag edge, leading to a high melting temperature in ²¹¹ the configuration. However, in Configuration 8 in ²¹² Table [1](#page-2-0) (43.88 A/Z edge ratio), the A/Z edge ratio is ²¹³ 43.88, proving that the armchair edge length is nearly ²¹⁴ 44 times longer than the zigzag one, leading to finite ²¹⁵ size effects in the melting process. Thus, to have a gen- 216 eral view of the influence of armchair and zigzag edge ²¹⁷ lengths, other A/Z ratios are larger than the one of ²¹⁸ Configuration 1 (0.0173770) and smaller than the one ²¹⁹ of Configuration 8 (43.88) (Table [1\)](#page-2-0). This means that ²²⁰ we need to consider Configurations 2 to 7 in Table [1](#page-2-0). 221 ii) Related to Configurations 2 to 7 in Table [1](#page-2-0), the A/Z 222 edge ratios range from 0.069510 to 10.745098. Within ²²³ this range of A/Z edge ratio, the melting temperature 224 point varies from 3900 to 4300 K (Figure [1](#page-3-0), Table [2\)](#page-4-0). 225 On average, the melting temperature within this ra- ²²⁶ tio range is approximately 4180 K. It can be observed 227

Figure 1: Total energy per atom (square symbol) and heat capacity (solid line) of armchair h-BNNR configurations containing 10,000 atoms in Table 1: a) Configuration 1: A/Z ratio is 0.017377, b) Configuration 2: A/Z ratio is 0.069510, c) Configuration 3: A/Z ratio is 0.278481, d) Configuration 4: A/Z ratio is 0.434782, e) Configuration 5: A/Z ratio is 1.724409, f) Configuration 6: A/Z ratio is 6.968254, and g) Configuration 7: A/Z ratio is 10.745098, h) Configuration 8: A/Z ratio is 43.88.

atoms. Configurations	$\mathbf{1}$	2	3	4	5	6		8
A/Z ratio	0.017377	0.069510	0.278481	0.434782	1.724409	6.968254	10.745098	43.88
Melting point (K)	5300	4200	3900	4360	4300	4100	4200	\cdot

Table 2: The melting point of different A/Z edge ratios of armchair h-BNNR configurations containing 10,000

 that the A/Z edge ratio does not significantly affect the melting temperature within this range. Specifi- cally, Configuration 2 (0.06951 A/Z edge ratio) and Configuration 7 (10.745098 A/Z edge ratio) in Table [1](#page-2-0) both exhibit a melting temperature of 4200 K (Ta- ble [2\)](#page-4-0). However, the total energy per atom of Con- figuration 7 is higher than Configuration 2 (Figure [2\)](#page-4-1). This may be because the Configuration 7 has a longer armchair edge length than Configuration 2, leading to the total energy per atom being higher (Tables 1 and 2, Figure [2](#page-4-1)). Thus, the melting temperature point of these two configurations (2 and 7) only differs very slightly from the average temperature point of the left six configurations in Table [1](#page-2-0) (from 2 to 7): 4200 K versus 4180 K. Therefore, it is necessary to investigate these two A/Z edge ratios to find a critical A/Z edge ratio. Note that, the melting point of the configuration having this critical A/Z edge ratio will not be affected much when the number of atoms in the configuration is increased.

Figure 2: Total energy per atom of armchair h-BNNR configurations containing 10,000 atoms: Configuration 2 in Table 1 (0.069510 A/Z edge ratio) – square symbols and Configuration 7 in Table 1 (10.745098 A/Z edge ratio) – circle symbols.

 First, for Configuration 2 in Table [1](#page-2-0) (A/Z ratio of 0.06951), the number of atoms in the configuration is increased from 10,000 atoms to 14,400, 19,600, and 25,600 atoms, but the A/Z ratio remains the same. Re-sults from the graph of total energy per atom show

that all of these configurations exhibit first-type phase 253 transition (Figure [3\)](#page-4-2). The phase transition temper- ²⁵⁴ atures of the 10,000, 14,400, 19,600, and 25,600 - ²⁵⁵ atom configurations are 4200, 3730, 3630, and 3520 ²⁵⁶ K, respectively. One can see that although the dif- ²⁵⁷ ference in the number of atoms between configura- ²⁵⁸ tions is about 5000 atoms, there is only a big dif- ²⁵⁹ ference in the phase transition temperature point of 260 the 10,000-atom configuration (4200 K) compared to $_{261}$ the 14,400, 19,600, and 25,600 -atom configurations $_{262}$ (3730, 3630, and 3520 K, respectively). The phase ²⁶³ transition temperature points of the left three config- ²⁶⁴ urations (14,400, 19,600, and 25,600 atoms) do not ²⁶⁵ fluctuate much even though the gap in the number 266 of atoms between configurations is also 5000 atoms. ²⁶⁷ Therefore, within the scope of this study, it can be con- 268 cluded that the phase transition temperature point of ²⁶⁹ the configurations having 0.06951 A/Z ratio is just rel- ²⁷⁰ atively stable when the number of atoms in the con- ²⁷¹ figuration is from 14,400 to 25,600. ²⁷²

Figure 3: Total energy per atom of armchair h-BNNR configurations with 0.06951 A/Z ratio: 10,000 atoms – square symbols, 14,400 atoms – circle symbols, 19,600 atoms –triangle symbols, and 25,600 atoms – star symbols.

As for Configuration 7 in Table [1](#page-2-0) (10.745098 A/Z ra- ²⁷³ tio), the number of atoms in the configuration also ²⁷⁴ increases from 10,000 atoms to 14,400, 19,600, and ²⁷⁵ 25,600 atoms but the A/Z ratio remains the same ²⁷⁶

 (10.745098). The melting temperature points of the 10,000, 14,400, 19,600, and 25,600-atom configura- tions are 4200, 3940, 4040, and 4040 K, respectively (Figure [4](#page-5-0)). This means that the melting temperature point of the 10.745098 A/Z case is not affected much by the number of atoms in the configuration even in case of $10,000$ atoms (Figure [4\)](#page-5-0). In particular, the melting temperature points of 19,600 and 25,600 - atom configurations are the same as shown in Figure [4](#page-5-0) (4040 K). It can be concluded that in the case of the 10.745098 A/Z ratio, the number of 10,000 atoms in the configuration has relatively ensured the stability of the phase transition temperature point. In addition, the noise of total energy in the 10.745098 A/Z con- figuration is less perturbed than the case of 0.06951 A/Z one (Figures [3](#page-4-2) and [4](#page-5-0)). The reason may be due to the armchair edge length in the case of 10.745098 A/Z ratio being large (Table [1\)](#page-2-0).

Figure 4: Total energy per atom of armchair h-BNNR configurations with 10.745098 A/Z ratio: 10,000 atoms – square symbols, 14,400 atoms – circle symbols, 19,600 atoms – triangle symbols, and 25,600 atoms – star symbols.

 Thus, within the scope of this study, in the case of the 10.745098 A/Z ratio, the configuration contain- ing 10,000 atoms is large enough to ensure the rela- tive stability of the phase transition temperature zone. Therefore, the 10.745098 A/Z ratio can be considered the critical A/Z edge ratio. The 10.745098 A/Z con- figuration can be visually observed before the melting temperature point (Figure [5a](#page-6-1)) and at the melting tem- perature point (Figure [5b](#page-6-1)). In addition to Configuration 8 in Table [1](#page-2-0) (43.88 A/Z ratio), several visualizations at different temperatures are shown to easily visualize the finite size effects. Based on the peaks in the heat capacity graph (solid

³⁰⁸ line in Figure 1h), several temperature values are cho-³⁰⁹ sen and presented in Figure [6.](#page-6-2) One can see that the crystal structures in this configuration break at a ³¹⁰ much lower temperature than those in the remaining 311 configurations in Table [1](#page-2-0) due to the finite size effects ³¹² $(Figure 6)$ $(Figure 6)$ $(Figure 6)$. 313

CONCLUSION 314

The melting process of armchair h-BNNR configura- ³¹⁵ tion containing 10,000 atoms is performed with dif- ³¹⁶ ferent A/Z ratios to study the dependence of the melt- ³¹⁷ ing process on the length of the armchair edges and to 318 find the critical A/Z ratio. The Tersoff potential is ap- ³¹⁹ plied to the interactions between B and N. 320

- To consider the dependence on A/Z ratios, eight dif- ³²¹ ferent A/Z ratio configurations (0.017377, 0.069510, ³²² 0.278481, 0.434782, 1.724409, 6.968254, 10.745098, ³²³ and 43.88) of armchair h-BNNR configuration con- ³²⁴ taining the same number of atoms (10,000 atoms) are 325 studied. The results show that the melting process is ³²⁶ strongly affected by the configurations with 0.017377 327 and 43.88 A/Z ratios. The former has a melting point 328 of 5300 K while the latter is affected by the finite size ³²⁹ effects. Related to the other configurations, the av- ³³⁰ erage value of melting point is 4180 K. And two of ³³¹ them (0.069510 and 10.745098 A/Z ratios) are chosen 332 to find the critical A/Z ratio because these two config- ³³³ urations have the same value of melting point (4200 ³³⁴ K) which is closed to the average melting point (4180 335 K). Note that, the melting point of the configuration 336 with this critical A/Z edge ratio will not be affected 337 much when the number of atoms in the configuration 338 is increased. 339

- To find the critical A/Z ratio, the A/Z ratios of the ³⁴⁰ two chosen configurations are fixed but the number ³⁴¹ of atoms in the configuration is increased from 10,000 ³⁴² to 14,400, 19,600, and 25,600 atoms for both 0.069510 343 and 10.745098 A/Z cases. The results show that the ³⁴⁴ 10.745098 A/Z ratio can be considered the critical A/Z ³⁴⁵ edge ratio because its melting point is not affected ³⁴⁶ much when the number of atoms is increased. In ad- ³⁴⁷ dition, the total energy of the 10.745098 A/Z ratio is ³⁴⁸ less noisy than the one of 0.069510 cases because long ³⁴⁹ the length of the armchair edges. 350

- The found critical A/Z ratio in this study can be the 351 benchmark for further experimental and theoretical 352 studies. 353

ABBREVIATIONS 354

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Figure 5: Three-dimensional view of armchair h-BNNR configuration having 10.745098 A/Z ratio at different values of temperature: a) 3000 K, b) 4200 K.

Figure 6: Three-dimensional view of armchair h-BNNR configuration having 43.88 A/Z ratio at different values of temperature: a) 2500 K, b) 4200 K, and c) 5400 K.

³⁵⁹ **AUTHOR'S CONTRIBUTIONS**

³⁶⁰ **FUNDING**

- **361 AVAILABILITY OF DATA AND** ³⁶² **MATERIALS**
- ³⁶³ Data and materials used and/or analyzed during the
- ³⁶⁴ current study are available from the corresponding
- ³⁶⁵ author on reasonable request.

³⁶⁶ **ETHICS APPROVAL AND CONSENT** ³⁶⁷ **TO PARTICIPATE**

³⁶⁸ Not applicable.

CONSENT FOR PUBLICATION 369

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